E. STRAUS 1921-1983

P. ERDÖS

Last July after I returned to Hungary from a meeting on number theory in the Netherlands, I heard the sad news that my friend and collaborator, E. Straus, died of a heart attack on July 12, 1983. I had known for a long time that he had diabetes and in fact we were together in 1948 in Princeton when this was diagnosed. I also knew that he had several earlier heart attacks. Nevertheless, I did not expect that the end would come so soon. I cannot write at such short notice a complete description of his far-reaching mathematical activities, so I will restrict myself to the history of our friendship and collaboration.

This is a very strong restriction since his most important work was probably on the connection between arithmetic and algebraic properties of entire functions, a subject about which I could only write after considerable preparation and for which there is now no time. Since I have been asked to finish this report in two to three weeks I must rely a great deal on my poor old memory. This last restriction is really my own fault; but, enough of the excuses, and let me start my subject. I will begin at the end. Let me state two of our relatively recent results which are "lost"; i.e., the proofs were supposed to be in more or less complete form in Ernst's possession, but we could find no trace of the manuscript and there is little hope that they can be found. Most likely they never existed. First, a result due to Ernst, Selfridge and myself.

Let $n > n_0(\varepsilon)$. Then

(1)
$$n! = a_1 a_2 \cdots a_n, \frac{n}{e} (1 - \varepsilon) < a_1 \le \cdots \le a_n$$

is always solvable in integers a_1, \ldots, a_n . This result is certainly not of great importance, nevertheless, it pleased us since it is the best possible. Since $n!^{1/n} = (1 + o(1)) (n/e)$, it is clear that in (1), $(n/e) (1 - \varepsilon) < a_1$ cannot be replaced by $(n/e) (1 + \varepsilon) < a_1$. Nevertheless, we managed to prove a slightly stronger form of (1). Let c be sufficiently large and $n > n_0(c)$. Then in (1), all the a's can be taken to be larger than $(n/e) (1 - c/\log n)$.

Ernst claimed that he had a nearly completed manuscript of the proof of (1). Perhaps this manuscript was lost or, perhaps, his memory deceived 332 P. ERDÖS

him. In any case, Selfridge and I will have to reconstruct our proof, which will be an onerous but not too difficult task. It might also be of some interest to determine the dependence of n_0 on ε ; e.g., determine the smallest n_0 so that for every $n > n_0$, n! is the product of n integers all greater than n/3. We have not yet carried out this task; but we hope to do so in time for our paper to be included in the collected papers of E. Straus, which I hope will be published in a few years.

Now to our second missing paper. This paper was supposed to have appeared in this Proceedings, and I should have prepared it after I heard of Ernst's death. Besides my laziness, I have an excuse; Ernst assured me that he had a nearly complete manuscript which was never found. Here is our result: Denote by F(n; k) the least common multiple of $n + 1, \ldots, n + k$ and by f(n; k) the least common multiple of $n - 1, n - 2, \ldots, n - k$. We would expect that usually F(n; k) > f(n; k) holds and, in fact if, say $k > \varepsilon n$, then for all, n, F(n; k) > f(n; k) is easy to see. We prove that for almost all n there is a k so that

$$(2) f(n; k) > F(n; k)$$

and conjectured with some trepidation that there are infinitely many integers n for which, for every k < n,

(3)
$$F(n; k) > f(n; k)$$

holds. We never came to a firm conclusion if (3) is true or not. It might be of some interest to try to determine the largest possible value of k = k(n) for which f(n; k) > F(n; h) can hold. It is easy to see that k must be o(n) but must it be $o(n^n)$? Also, can one estimate the number of integers k for which (2) holds? We planned to investigate this in the future, but, unfortunately, fate prevented us. These problems are probably not of great importance; but it often happened before that seemingly special questions in number theory unexpectedly lead to interesting developments.

Now let me come back to the beginning. In 1944 Ernst Straus visited me with his fiancee, Louise, in Princeton. He was interested in various geometric problems about convex sets. These problems are not very popular now, but let me mention only one question which we then discussed and which is still open. Let J be a Jordan curve. Is it always possible to find four points on J which are the vertices of a square? I do not know who first formulated this pretty conjecture, and as far as I know it is still open. Let me add a little story which I remember. We had lunch together with the great algebraist Claude Chevalley, who was never much interested in elementary geometry but noticed "bosses", i.e., girls. He said about Louise: "What a pretty girl, I hope we will see more of her".

Our next contact with the Strauses was in the summer of 1948. Louise and Ernst were married by then and all three of us were in Princeton. We then made the following pretty conjecture. Is it true that, for every integer n, 4/n = 1/x + 1/y + 1/z is solvable in positive integers x, y, z? This interesting conjecture is still open. It is settled for many arithmetic progressions and also, if it fails, then the smallest such n must be quite large. Schinzel and Sierpinski have the following extension. For every a there is an $n_0(a)$ so that, for every $n > n_0(a)$,

$$\frac{a}{n} = \frac{1}{x} + \frac{1}{y} + \frac{1}{z}$$

is solvable in positive integers x, y, z. In memory of Straus, I offer five hundred dollars for a proof or disproof of this conjecture.

The paper On the representation of fractions as sum and difference of three simple fractions (Jointly with M.V. Subbarao), deals with the Schinzel conjecture that, for every given positive integer a and all sufficiently large n, the equation $a/n = 1/x \pm 1/y \pm 1/z$ has integral solutions x, y, z. It has been proved there that the conjecture holds for all a less than 40, and that at least in the cases $a \le 35$, the fraction 1/x can be chosen among the three nearest neighbours of a/n. Further, the paper gives some conjectures each of which implies the Schinzel conjecture. One such conjecture states that

$$\lim_{n\to\infty}\sup_{s\geq0}\frac{d(n+s)}{s+1}=\infty.$$

Our first joint paper was in fact written when we both were at UCLA, Ernst was at the University of California and I at the Institute for Numerical Analysis. I have to add here a personal note (perhaps when my obiturary will be written (soon?) this should be mentioned). John Curtiss was then head of the Institute for Numerical Analysis and he created for me the so called Curtiss condition, i.e., I was paid only when I was there and I could leave without asking for a leave of absence but it was up to the Institute to decide if I got paid while I was away (since then I have been fortunate enough to have posts only under these conditions).

In our paper we answer the following question of Dvoretsky. Let x_1 , x_2 , ... be an infinite sequence of unit vectors in a Banach space which are linearly independent in the algebraic sense. Is it then true that there is a subsequence which is linearly independent in a stronger sense? We prove, among other things, that there always is a subsequence for which $\sum_{i=1}^{\infty} \langle n_i x_{n_i} \rangle = 0$ implies $\langle n_i \rangle = 0$.

We were together again in Colorado in 1959 and 1963. We proved the following theorems: Let n_h be an increasing sequence of positive integers and assume $\lim\sup n_h^2/n_{h+1} \leq 1$, $N_h < cn_{h+1}$ where N_h is the least common multiple of n_1, \ldots, n_h . Then $\sum 1/n_h$ is rational only if $n_{h+1} = n_h^2 - n_h + 1$ for all $h > h_0$. It is not impossible that the conditions $N_h < Cn_{h+1}$ are

334 P. ERDÖS

superfluous. We could weaken it but could not eliminate it entirely. We wrote several more papers on the irrationality of infinite series. Here I mention only one problem of ours which has never been published.

It is easy to see that if $n_1 \le \cdots$ is a sequence of integers for which $\sum_{k=1}^{\infty} 1/n_k$ is rational, then we must have

$$\lim n_k^{1/2^k} < \infty$$

and this is best possible. Let

$$\sum_{k=1}^{\infty} \frac{1}{n_k} \text{ and } \sum_{k=1}^{\infty} \frac{1}{n_k - 1}$$

both be rational. How fast can n_k increase? David Cantor observed that this holds for $n_k = \binom{k}{2}$ and we could never decide if n_k can increase exponentially or even faster. We observed that the set of points (x, y) in the plane $(n_1 < n_2 < \cdots, n_k$ integers), given by

$$x = \sum_{k} \frac{1}{n_k}, y = \sum_{k} \frac{1}{n_k - 1},$$

contains open sets and this no doubt generalises for higher dimensions. Perhaps we missed the nicest conjecture (due to Stolarsky) which states as follows. Let $n_1 < n_2 < \cdots$ be an infinite sequence for which $\sum 1/n_k < \infty$.

Is it then true that there is an integer t for which $\sum_{n_k \neq t} 1/(n_k - t)$ is irrational?

Straus and I also considered the following question. Let a sequence $A: a_1 < a_2 < \ldots$ be called non-averaging if the arithmetic mean of any two or more members of A is not in A. What can be said about the growth properties of such sequences? We proved that if $a_1 < a_2 < \cdots < a_k \le n$ then $k = o(n^{2/3})$ and conjectured that $k < n^s$ for every $\varepsilon > 0$. This was shown to be false by H. L. Abbott who showed that it is possible to have $k \ge n^{1/10}$. Recently, Abbott improved this to $n^{1/5}$. Many interesting open questions remain here. (H. L. Abbott, On a conjecture of Erdös and Straus on non-averaging sets of integers, Proc. Fifth British Combinatorial Conference, Congressus Numerantium XV, (1975), 1–4).

In 1959 at the meeting at Boulder, Colorado, Bose, Parker and Shrikhande presented their disproof of Euler's conjecture, i.e., they proved that, for every n > 6, there are two pairwise orthogonal Latin squares. Inspired by their ideas, Chowla, Straus & I showed that the number of pairwise orthogonal Latin squares of order n is greater than cn^{ϵ} where our ϵ was > 1/91. R. Wilson considerably improved our result but perhaps further improvement will be possible in the future.

Now I discuss what I think is our most important and most original joint work, namely our papers on Euclidean Ramsey Theorems. I hope that these results, and even more the problems, will outlive the authors,

hopefully, by centuries. A set k of Euclidean m space is called Ramsey if, for every r, there is an $n = n_0(k, r)$ so that, for every r coloring of Euclidean n space, there is a monochromatic configuration k' which is congruent to k. If congruent is replaced by similar, then Gallai proved that every finite set k is Ramsey. In our first paper on this subject we prove that every brick, i.e., every rectangular parallelepiped is Ramsey and we also prove that every set which is Ramsey must lie on an m dimensional sphere. We never could decide whether any of these conditions are necessary or sufficient. It is quite possible that the truth is somewhere in between. Perhaps the most interesting open problems are: Is the regular pentagon Ramsey? or is every triangle Ramsey or, in particular, is the triangle of angles 30, 30, 120 Ramsev (every acute angled triangle is the subset of a brick and is therefore Ramsey)? Also is it true that if we divide the plane into two subsets and T is any triangle, then at least one of the subsets contains a monochromatic congruent copy of T (i.e., the vertices of T) with a possible single exception of an equilateral T. We and L. Shader proved several special cases of this conjecture. As another nice problem, let S be a set in the plane, no two points of which are at distance 1. Is it then true that the complement \bar{S} of S contains the vertices of a square? R. Juhasz proved our conjecture in a more general form. She proved that \bar{S} contains a congruent copy of any configuration of four points. She further showed that four cannot be replaced by 12, but the exact value of this number is not known, e.g., is it true for 5? (R. Juhasz, Ramsey type theorems in the plane, J. Combinatorial Theory (1979), 152-170.)

To end this short obituary I just want to remark that Ernst was not only a first rate mathematician, but also a superior human being, both intellectually and morally. I remember one occasion when, with great tact, insight and intelligence, he smoothed over a potentially unpleasant disagreement between two excellent mathematicians. I was concerned since they were both friends of mine and I wrote congratulating him for a success which had cluded me. "Blessed are the peace makers". UCLA, Los Angeles, California and the world will never be the same for me without him. May his theorems live forever.

PUBLICATION LIST

E. G. Straus and Albert Einstein, The influence of the expansion of space on the gravitation fields surrounding the individual stars, Rev. Modern Physics 17 (1945), 120-124.

and — , Corrections and additional remarks of our paper: The influence
of the expansion of space on the gravitation fields surrounding the individual stars, Rev.
Modern Physica 18 (1946), 148–149.

- and ______, A generalization of the relativistic theory of gravitations II, Ann. Math. 47 (1946), 731–741.
- Some results in Einstein's unified field theory, Rev. Modern Physics 21 (1949), 414-420.
- and R. Bellman, Continued fractions, algebraic functions and the Padé Table, Proc. Nat. Acad. Sci. 35 (1949), 472–476.
- On entire functions with algebraic derivatives at certain algebraic points, Ann. Math. 52 (1950), 188–198.
- On a class of integral-valued Dirichelt series, Proc. International Congress Math. 1 (1950), 423.
- and S. P. Diliberto, On approximating to functions of several variables by functions of fewer variables, Proc. International Congress Math. 11 (1950), 378.
- On the polynomials whose derivatives have integral values at the integers, Proc. Amer. Math. Soc. 2 (1951), 24–27.
- and S. P. Diliberto, On the approximation of a function of several variables by the sum of functions of fewer variables, Pac. J. Math. 1 (1951), 195–210.
- Functions periodic modulo each of a sequence of integers Duke Math, J. 19 (1952), 379–395.
- and F. A. Valentine, A characterization of finite dimensional convex sets, Amer. J. Math LXXIV (1952), 683–686.
- 13. —, T. S. Motzkin and —, The number of farthest points, Pac. J. Math. 3 (1953), 221-232.
- and P. Erdos, On linear independence of sequences in a Banach space, Pac. J. Math. 3 (1953), 689-694.
- —, K. Goldberg, M. Newman and J. D. Swift, The representation of integers by binary quadratic rational forms, Archiv der Mathematik 5 (1954), 12–18.
- and G. E. Forsythe, On best conditioned matrices, Proc. A. M. S. 6 (1955), 340–345.
- and J. D. Swift, The representation of integers by certain rational forms, Amer, J. Math. 78 (1956), 62-70.
- 18. , A. J. Hoffman, M. Newman and O. Taussky, On the number of absolute points of correlation, Pac. J. Math. (1956), 83-96.
- and O. Taussky, Remark on the preceding paper; Algebraic equations satisfied by roots of natural numbers, Pac. J. Math. 6 (1956), 97–98.
- Assistant bei A. Einstein (in a book of essays about A. Einstein, Helle Zeit, dunkele Zeit) Zurich, 1956.
- Einstein the man (collected speeches given at memorial meeting at UCLA under title "A. Einstein Memorial") Los Angeles, 1956.
- and T. S. Motzkin, Some combinatorial extremum problems Proc. A.M.S. 7 (1956), 1014–1021.
- and Paul Kelly, A characteristic property of the circle, ellipse, and hyperbola, Amer. Math. Monthly 63 (1956) 710–711.
- On a problem of W. Sierpinski on the congruence of sets, Fundamenta Mathematicae 44 (1956), 75-81.
- and P. J. Kelly, Inversive and conformal convexity, Proc. Amer. Math. Soc. 8 (1957), 572–577.
 - 26. and B. O'Neill, A fixed point theorem, Proc. A.M.S. 8 (1957), 1148-1151.
- and G. Szekeres, On a problem of D. R. Hughes, Proc. A.M.S. 9 (1958), 157-158.
- 28. and Paul Kelly, Curvature in Hilbert geometries, Pac. J. Math. 8 (1958), 119-125.

- On Sierpiński sets in groups, Fundamenta Mathematicae 45 (1958), 332–333.
- 30. and G. K. Kalisch, On the determination of points in a Banach space by their distances from the points of a given set, Am. Acad. Brasil. Ci. 29 (1958), 501-519.
- and J. Selfridge, On the determination of numbers by their sums of a fixed order, Pac. J. Math. 8 (1958), 847–456.
- 32. , C. J. A. Halberg, Jr., and E. Levin, On contiguous congruent sets in Euclidean space, Proc. A.M.S. 10 (1959), 335-344.
- 33. , S. Chowla and H. Mann, Some applications of the Cauchy-Davenport theorem, Forh. Norsk. Vid. Selsk. 32 (1959), 74-80.
- 34. —, A functional equation proposed by R. Bellman, Proc. A.M.S. 10 (1959), 860-862.
 - 35. and H. Busemann, Area and normality, Pac. J. Math 10 (1960), 35-72.
- and K. Rogers, A class of geometric lattices, Bull. A.M.S. 66 (1960), 118– 123.
- S. Chowla and P. Erdos, On the maximal number of pairwise orthogonal Latin squares of a given order, Can. J. Math. 12 (1960) 204–208.
- 38. and P. Kelly, On the projective centres of convex curves Can. J. Math. 12 (1960), 568-581.
- J. Aczel and M. Hosszu, Functional equation for products and compositions of functions, Pub. Math. Debrecen 8 (1961), 218–224.
- R. Sacksteder and F. A. Valentine, A generalization of a theorem of Tietze and Nakajima on local convexity, J. London Soc. 36 (1961), 52–56.
- —, L. Carlitz, D. J. Lewis and W. H. Mills, Polynomials over finite fields with minimal value sets, Mathematika 9 (1961) 121–130.
- and T. S. Motzkin, Representation of a point of a set as sum of transforms of boundary points, Proc. Symposium on Convexity, Seattle, 1961.
- 43. , B. Gordon and A. S. Fraenkel, On the determination of sets of sums of a certain order, Pac. J. Math. 12 (1962) 187-196.
 - 44. ----, On a problem in the theory of partitions, Proc. A.M.S. 13 (1962), 192-196.
- and K. Rogers, A special class of matrices, Pac. J. Math. 12 (1962), 699– 707.
- and T. S. Motzkin, Representation of a point of a set as sum of transforms of boundary points, Pac. J. Math. 13 (1963) 633-637.
- Two comments on Dvoretzky's sphericity theorem, Israel J. Math 1 (1963), 221–223.
- and P. Erdos, On the irrationality of certain Ahmes series J. Indian Math. Soc. 1964.
 - 49. and R. Redheffer, Degenerate elliptic equations, Pac. J. Math. 14 (1964).
 - and P. Katz, Infinite sums in algebraic structures Pac. J. Math. 14 (1964).
- P. Erdos, B. Gordon and L. A. Rubel, Tauberian theorems for sum sets, Acta Aritmetica 9 (1964), 177-189.
- and Diahachiro Sato, Rate of growth of Hurwitz entire functions and integer valued entire functions, Bull. of Amer. Math. Soc. 70 (1964), 303–307.
- and B. Gordon, On the degrees of the finite extensions of a field, Proc. Symp. Pure Math. VIII (1965), 56-65.
- Rational dependence in finite sets of numbers, Acta Arithmetica 11 (1965), 203–204.
- and D. Sato, On the rate of growth of Hurwitz functions of a complex or p-adic variable, J. of Math. Soc. of Japan 17 (1965), 17–29.

- and T. S. Motzkin, Maxima for graphs and a new proof of a theorem of Turan, Canadian J. Math. 17 (1965), 533-540.
- and L. A. Rubel, Special trignometric series and the Riemann hypothesis, Math. Scand. 18 (1966), 35–44.
- On a problem of R. Bellman, J. Math. Analysis and Applications 14 (1966), 427–432.
- and D. Sato, Generalized interpolation by analytic functions, Bull of Amer. Math. Soc. 72 (1966), 32–36.
- On a problem in combinatorial number theory, J. of Math Sciences 1 (1966), 77–80.
- and D. Sato, Generalized interpolation by analytic functions, J. of Math. Sciences 1 (1966), 53-76.
- Uber eine geometrishee Frage von Fejes-Toth, Elemente der Mathematik, Band 23 (1968), 11-14.
- and P. Kelly, Curvature in Hilbert geometries II, Pac. J. Math. 25 (1968), 549–552.
- D. G. Cantor and D. L. Hilliker, Interpolation by analytic functions of bounded growth, Aequationes Mathematicae 2 (1969), 337–347.
- and L. D. Neidleman, Functions whose derivatives at one point form a finite set, Trans. of A.M.S. 140 (1969), 411–422.
- and T. S. Motzkin, Divisors of polynomials and power series with positive coefficients, Pac. J. Math. 29 (1969) 641-652.
- and P. Erdös, Nonaveraging sets II, Colloquia Mathematica Societatis Janos Bolyai, (Hungary) (1969), 405–411.
- and Paul Kelly, Elements of Analytic Geometry, Scott Foresman and Company, Illinois, 1970.
- Some p-adic versions of Polya's theorem on integer valued analytic functions, Proc. AMS 26 (1970), 395–400.
- and W. W. Adams, Non-archimedian analytic functions taking the same values at the points, Illinois J. of Math., 15 (1971), 418–424.
- Nonaveraging sets, Amer. Math. Soc. Proc. of Symposium on Pure Math, 12 (1969), 215–222.
- and P. Erdös, Some number theoretic results, Pac. J. Math. 36 (1971) 635–646.
- and H. G. Senge, PV-numbers and sets of multiplicity, Acta Arithmetica (1972). (Also appeared in Proc. of the Washington State U. Conference on Number Theory) (1971), 55-67.
- —, Differential rings of meromorphic functions, Acta Arithmetica 21 (1972), 271–284.
- ——, Differential rings of analytic functions of a non-Archimedean variable, in Diophantine Approximation and its Applications, Academic Press New York, 1973. 295– 308.
- Representation of positive analytic functions as ratios of absolutely monotonoic functions, in Spline Functions and Approximation Theory, Birkhäuser, Cambridge, 1973, 359–270.
- T. S. Motzkin and A. Sharma, Averaging interpolation in Spline Functions and Approximation Theory, Birkhäuser, Cambridge, 1973, 191–233.
- P. Erdös, R. Graham, P. Montgomery, B. Rothschild, and J. Spencer, Euclidean Ramsey theorems I, J. Combinatorial Theory 14 (1973), 341–363.
- 79. —, —, —, and —, Euclidean Ramsey theorems, II, Colloquia Mathematica Societatis Janos Bolyai (Hungary) (1973), 529–557.

- P. Erdös, L. Lovasz, G. Simmons Dissection graphs of planar point sets, in A Survey of Combinatorial Theory, North-Holland (1973), 139–149.
- T. S. Motzkin and B. O'Neill, Isolated subgroups, Michigan J. Math 20 (1973), 235–248.
- 83. _____, On the greatest common divisor of binomial coefficients Fibonacci Quarterly 11 (1973), 25-26.
- 84. ——, R. L. Graham and B. Rothschild, Are there n + 2 points in Eⁿ with odd integral distances?, Amer. Math. Monthly 81 (1974), 21-25.
- 85. , B. Bollobas and P. Erdos, Complete subgraphs of chromatic graphs and hypergraphs, Utilitas Mathematica, 6 (1974), 343-347.
- 86. —, Some applications of a non-Archimedean analogue of Descartes rule of signs, Acta Arithmetica 25 (1974), 353-357.
- 87. and A. Sharma, On the irreducibility of a class of Euler-Frobenius polynomials, Can. Bull. Math 17 (1974), 265-273.
- —, Ideals in near-rings of polynomials over a field, Pac. J. Math 52 (1974), 601–603.
- and P. Erdös, On the irrationality of certain series, Pac. J. Math. 55 (1974), 85–92.
 - 90. and J. Arkin, Latin k-cubes, Fibonacci Quarterly 12 (1974), 287-292.
- —— and M. V. Subbarao, On exponential divisors, Duke Math. J. 41 (1974), 465-571.
- A combinatorial theorem in group theory, Mathematics of Computation 29 (1975), 303–309.
- and A. H. Cayford, On differential rings of entire functions, Trans. of the A.M.S. 209 (1975), 283–293.
- P. Erdős, R. L. Graham, I. Z. Ruzsa, On the prime factors of (2^{nk}), Math. of Computation 29 (1975), 83–92.
 - 95. , Differences of residues (mod p), J. of Number Theory 8 (1976), 40-42.
- and P. Erdös, How Abelian is a finite group?, Linear and Multilinear Algebra 3 (1976), 307–312.
- L. H. Harper, T. H. Payne, and J. E. Savage, Sorting X + Y, A.C.M. Journal (1976).
- Joseph Arkin and Verner E. Hoggatt, Jr. Systems of magic Latin k-cubes, Can. J. Math. 29 (1976), 1153–1161.
- and Moshe Goldberg, Inclusion relations involving k-numerical ranges, Linear Algebra and Its Applications 15 (1976), 261–270.
- 100. and Demetrios Brizolis, A basis for the ring of doubly integer-valued polynomials, Journal fur die Reine und Angewandte Mathematik (1976), 187–195.
- and Moshe Goldberg, On a theorem by Mirman, Linear and Multilinear Algebra 5 (1977), 77–78.
- 102. and , On characterizations and integrals of generalized numerical ranges, Pac. J. Math. 69 (1977), 45-54.
- 103. and , Elementary inclusion relations for generalized numerical ranges, Linear Algebra and its Applications 18 (1977), 1-24.
- 104. and P. Erdös, On products of consecutive integers, in Number Theory and Algebra, Academic Press, New York, 1977, 63–70.
- 105. and G. Kolesnik, On the first occurrence of values of a character, Trans. of the A.M.S. 246 (1978), 385-394.
 - 106. and M. V. Subbarao, On the representation of fractions as sum and differ-

- ence of three simple fractions, Proc. Seventh Manitoba Conf. on Numerical Math. and Computing, 1977, Utilitas Math. (1978), 561-579.
- and Moshe Goldberg, Norm properties of C-numerical radii, Linear Algebra and Its Applications 24 (1979), 113–131.
- Joseph Arkin and V. E. Hoggatt, Jr., On Euler's solution of a problem of Diophantus, Fibonacci Quart 17 (1979), 333–339.
- and Moshe Goldberg, Combinatorial inequalities, matrix norms, and generalized numerical radii, General Inequalities 2, Birkhäuser Verlag, Basel (1980), 37–46.
- Joseph Arkin and V. E. Hoggatt, Jr., On a problem of Diophantus II, Fibonacci Quarterly 18 (1980), 170-176.
- and P. Erdos, Remarks on the differences between consecutive primes, Elemente der Mathematik 35 (1980), 115–118.
- and G. Kolesnik, On the distribution of integers with a given number of prime factors, Acta Arithmetica 37 (1980), 181–199.
- 113. and Joseph Arkin, Orthogonal Latin systems, Fibonacci Quarterly 19 (1981), 289-293.
- 114. and P. T. Bateman, P. Erdös, and C. Pomerance, The arithmetic mean of the divisors of an interger, Lecture Notes in Math. 899 (1981), 197–220.
- 115. _____, V. G. Kane and S. P. Mohanty, Which rational numbers are binding numbers? J. Graph Theory 5 (1981), 379-384.
- 116, —, P. Erdos and G. Purdy, On a problem in combinatorial gemoetry, Discrete Math. 40 (1982), 45-52.
 - 117. and A. W. Hales, Projective colorings, Pacific J. Math. 99 (1982), 31-43.
- and Moshe Goldberg, Operator norms, multiplicativity factors, and C-numerical radii, Linear Algebra and Appl. 43 (1982), 137–159.
- and Vera T. Sos, Externals of functions on graphs with applications to graphs and hypergraphs, Combinatorial Theory Ser. B 32 (1982), 246–257.
- (review) A Simple Non-Euclidean Geometry and its Physical Basis, by
 M. Yaglom, Amer. Math. Monthly 89 (1982), 510-513.

PAPERS SUBMITTED OR ACCEPTED FOR PUBLICATION

- and G. Kolesnik, On the sum of powers of complex numbers, to appear in Turan Volume of Hungarian Academy of Sciences.
- and D. G. Cantor, On a conjecture of D. H. Lehmer to appear in Acta Arithmetics.
- 3. P. Erdos and B. Rothschild, Polychromatic Euclidean Ramsey theorems, to appear in J. Geometry.
- and Moshe Goldberg, Combinatorial inequalities, matrix norms, and generalized numerical radii II, to appear in General Inequalities, edited by E. F. Beckenbach.
- 5. and David Lee Hilliker, On Puiseux series whose curves pass through an infinity of algebraic lattice points, to appear in Bull. Amer. Math. Soc.
- and P. Lockhart, Entire functions which are infinitely integer-valued at a finite number of points, submitted to Trans. Amer. Math. Soc.
- and David Lee Hilliker, Determination of bounds for the solutions to those binary diophantine equations that satisfy the hypotheses of Runge's theorem, submitted to Trans, Amer. Math. Soc.
- 8. and M. Goldberg, On generalizations of the Perron-Frobenius theorem, to appear in LAMA.
 - and , Multiplicativity factors for C-numerical radii, to appear in LAA.

and ——, Multiplicativity of /, norms for matrices, to appear in LAA.
 Mathematical Institute of the Hungarian Academ yof Sciences, Budapest, Hungary

ADDED IN PROOF. P. Frankl and V. Rodl proved that every triangle is Ramsey.